# NPS Learning in Place Geometry



Week 1	Equation of circles
April 6-10	Day 1 - 5
Week 2	Circles Continue
April 20-24	Day 6 - 10

Name	School	Teacher	
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## **STANDARD FORM OF THE EQUATION OF A CIRCLE**

EQUATION	EXAMPLE	GRAPH
The equation of a circle with center $(h, k)$ and radius <b>r</b> is $(x - h)^2 + (y - k)^2 = r^2$ .	The equation of the circle with center $(5, -2)$ and radius $r = 8$ is $(x - 5)^2 + (y - (-2))^2 = 8^2$ or $(x - 5)^2 + (y + 2)^2 = 64.$	-4 0 4 8 12 -4 (h, k) -8

## **Helpful Hint**

If the center of the circle is at the origin, the equation simplifies to  $x^2 + y^2 = r^2$ .

Example 1: Write the equation o with center (-3, 4) and radius r =	f a circle 6.	Example 2: Write the equation of the circle with center (0,6) and a diameter of 2.
Center: (h,k) $\rightarrow$ (-3, 4) radius: r $\rightarrow$ 6	r <sup>2</sup> = (6)(6) = 36	Center: (h,k) $\rightarrow$ (0, 6) d = 2 radius: r $\rightarrow \frac{d}{d} = 1$ r <sup>2</sup> = (1)(1) = 1
Formula: $(x - h)^2 + (y - k)^2 = r^2$ $(x - (-3))^2 + (y - 4)^2 = 6^2$ $(x + 3)^2 + (y - 4)^2 = 36$		Formula: $(\mathbf{x} - \mathbf{h})^2 + (\mathbf{y} - \mathbf{k})^2 = \mathbf{r}^2$ $(\mathbf{x} - 0)^2 + (\mathbf{y} - 6)^2 = 1^2$ $\mathbf{x}^2 + (\mathbf{y} - 4)^2 = 1$

Example 3: Write the equation of a circle with center (-2,-5) and radius r =  $\sqrt{12}$ 

Center: (h,k)  $\rightarrow$  (-2, -5) radius: r  $\rightarrow \sqrt{12}$  r<sup>2</sup> =  $(\sqrt{12})^2$  = 12

Formula:  $(x - h)^2 + (y - k)^2 = r^2$  $(x - (-2))^2 + (y - (-5))^2 = (\sqrt{12})^2$  $(x + 2)^2 + (y + 5)^2 = 12$ 

## Equation of Circles Day 1

Directions: Write the equation of the circle			
1. radius: 2 center: (4, 6).	2. radius: 8 center: (0, 9)	3. radius: 3 center: (6, - 2).	
4. diameter: 10 center: (-4, 0).	5. diameter: 18 center: (-2, -5)	6. diameter: 24 center: (-3, -1).	
7 diameter: 15 center: (0,0)	8. radius √47 Center: (0, -5)	9. radius: √15 Center: (0, -5)	
10. radius: 4 Center: (-1,3) (h,k) 4 r: 4			

#### Notes

Write the equation of a circle given the center and a point on the circle.

Step 1: Find the radius using the distance formula or the Pythagorean TheoremStep 2: Substitute the center and the radius into the formula

Example: Write the standard form of the equation of the circle that passes through the point (2, -1) and whose center is on the origin (0,0).



## Equation of a Circle given the center and a point on the circle-Day 2

Directions: Write the equation of a circl	e given a point on the circle and the
center	
1. Center: (9, 10), Point on Circle: (7, 4)	2. Center: (1, -5), Point on Circle: (-7, -13)
3. Center: (2, -6); Point on Circle: (1, 10)	4. Center: (-2, 0); Point on Circle: (-9, -4)
5. Center: (–13, –16); Point on Circle: (–10, –16)	6. Center: (3, -4); Point on Circle (6, 2).
7. Center: (5, 1); Point on the circle (8, -2).	8. Center: origin; Point on Circle (4, 3).
9.	

#### Notes

#### Write the equation of a circle given the center and a point on the circle.

Step 1: Find the center using the midpoint

**Step 2:** Find the radius using the coordinates of the center and a point on the circle

Step 3: Substitute the center and the radius into the formula

Example: Write the standard form of the equation of the circle with a diameter with endpoints (-2, 1) and (4, 3).

Step 1: Midpoint	Step 2: Pythagorean Theorem-	Step 3: Substitute into the equation of a circle	
Midpoint: Center of circle	Hint: Must use the center	Write the equation of the circle	
Midpoint: $(\frac{x_2+x_1}{2}, \frac{y_{2+y_1}}{2})$	XY	Center: (h,k) → (1,2)	
Points: $(-2, 1)$ and $(4, 3)$	4-1 3=a <b>1 2</b> 3-2 1=b	r <sup>2</sup> = 5	
		Formula: (x – h)² + (y – k)² = r²	
Center: $(\frac{4+(-2)}{2}, \frac{3+1}{2})$	$a^2 + b^2 = c^2$	$(x-1)^2 + (y-2)^2 = 10$	
Center: $(\frac{2}{4}, \frac{4}{4})$	$c = radius$ $c^2 = r^2$		
2 2	$(3)^2 + (1)^2 = r^2$ 9 + 1 = r <sup>2</sup>		
Center: ( 1, 2)	$10 = r^2$		

You Try it: Write the standard form of the equation of the circle with a diameter with endpoints (8, -7) and (4, 5).

Step 1: Midpoint	Step 2: Pythagorean theorem	Step 3: Substitute into the equation of a circle

## Equation of a Circle given the endpoints of the diameter-Day 3

Directions: Write the equation of a circl	le given the endpoints of the diameter
1. Write the equation of a circle with diameter	2. Write the equation of a circle with diameter
endpoints of (13, -1) and (-15, 9)	endpoints of (-5, 2) and (3, 6)
3. Write the equation of a circle with diameter	4. Write the equation of a circle with diameter
endpoints of (5, 4) and (-1, -6)	endpoints of (-2, 1) and (8, 9)
5. Write the equation of a circle with diameter	6. Write the equation of a circle with diameter
endpoints of (-6, 7) and (4, 1)	endpoints of (2, 8) and (2, -2)
7. Write the equation of a circle with diameter	8. Write the equation of a circle with diameter
endpoints of (10, -6) and (-6, 10)	endpoints of (1, 2) and (-1, -6)
9.	10.
A = (-4, 2)	B(4,12)
B = (4, -6)	A(-2,4)



<b>Directions:</b> G	iven the equa	ation of the ci	rcle, determ	ine if the po	oint is on,
inside, or out	side the circl	e.			
1. $x^2 + (y - 4)^2 = 4$	9 point	(0, 11)	2. $(x + 6)^2 + (y - 6)^2$	+ 3) <sup>2</sup> = 25 p	oint (-2, 1)
on	inside	outside	on	inside	outside
3. (x - 7) <sup>2</sup> + (y - 1	) <sup>2</sup> = 16 poi	nt (12,6)	4. (x - 5) <sup>2</sup> + (y -	1) <sup>2</sup> = 9 p	oint (6, 0)
on	inside	outside	on	inside	outside
5. (x - 5) <sup>2</sup> + (y - 1) <sup>2</sup>	= 9 point	(8, 2)	6. (x - 2) <sup>2</sup> + (y +	3) <sup>2</sup> = 4	Point (3, -1)
on	inside	outside	on	inside	outside
<ul> <li>7. The center of a circle is (-3, 0) and its radius is 5.</li> <li>Which point does NOT line on the circle?</li> <li>A. (2, 0)</li> <li>B. (0, 4)</li> <li>C. (-3, 0)</li> <li>D. (-3, -5)</li> <li>9. Which of these points lie on the circle represented</li> </ul>		8. Circle O has a units. Which poi A. (3, 4) B. (-3, -1) C. (5, 1) D. (8, 0) 10. A circle has	a center at (3, 1) a nt lies on circle O <b>a center at (-1,</b>	nd a diameter of 10 ? <b>4) and a diameter of</b>	
by this equation? $(x - 4)^2 + (y + 3)^2 =$ (-4, 3)	10 <sup>2</sup>	(4,7)	20. Select each point on this ci	(11, 20) (:	ates that represent a
(4, -3) (10, 5)		(5, 12)	(-9, -2)	(-1, 4)	

Notes				
Formula: $(x \ominus h)^2 + (y \ominus k)^2 = r^2$				
HINT: Notice the operation inse the parentheis is sub subtraction, you must rewrite the equation using sub	traction. If the operation is not traction			
Step 1: Is the operation inside parenthesis Subtractio	n			
YES!	NO!			
The center is represented by the number following the subtraction.	Rewrite the equation using subtraction.			
Step 2: Take the square root of r <sup>2</sup> to find the radius. Step 3: Double the radius to find the diameter.				
<b>Example 1:</b> $(x-2)^2 + (y-3)^2 = 25$ . (a) Find the center	, radius and diameter			
<b>Step 1:</b> Is the operation inside the parenthesis subtra Center: (2, 3)	ction? Yes			
<b>Step 2:</b> $r^2 = 25$ $r = \sqrt{25}$				
r = 5 Diameter: (2)(5) = 10				
<b>Example 2:</b> $(x - 3)^2 + (y + 6)^2 = 81$ (a) Find the cente	r, radius and diameter			
<b>Step 1:</b> Is the operation inside the parenthesis subtraction. (x - 3) <sup>2</sup> + (y - (-6)) <sup>2</sup> = 81 Center: (3, -6)	ction? <b>Yes</b> for the x, NO for the y. Rewrite the y as a			
<b>Step 2:</b> r <sup>2</sup> = 81				
$r = \sqrt{81}$				
Example 3: $x^{2} + (y - 3)^{2} = 30$ $(x - 0)^{2} + (y - 3)^{2} = 30$				
<b>Step 1:</b> Is the operation inside the parenthesis subtracenter: (0, 3)	ction? <b>Yes</b>			
<b>Step 2:</b> r <sup>2</sup> = 30				
r = $\sqrt{30}$ Diameter: (2)( $\sqrt{30}$	$) = 2\sqrt{30}$			

## Determine parts of a circle given the Equation-Day 5

Directions: Given the equation of the ci	rcle, determine the center, radius and
diameter 1 $(y = 0)^2 + (y = 4)^2 = 36$	$2(x+1)^2 + (y-1)^2 - 106$
1. (X 3) · (Y 4) = 30	2. (x + 1) + (y + 1) = 130
Center:	Center:
Radius:	Radius:
Diameter:	Diameter:
3. $(x + 6)^2 + y^2 = 90.25$	4. $(x - 2)^2 + (y + 13)^2 = 150$
Center:	Center:
Radius:	Radius:
Diameter:	Diameter:
5. $(x - 1)^2 + (y + 4)^2 = 169$	6. $x^2 + y^2 = 16$
Center:	Center:
Radius:	Radius:
Diameter:	Diameter:
7. The equation of a circle is $(x + 2)^2 + (y + 7)^2 = 49$ .	8. The equation of a circle is $(x - 3)^2 + (y + 4)^2 = 16$
What is the center of the circle?	a) What is the coordinate of the center of the circle?
A. (2, 7)	
B. (-2, 7)	b) What is the radius of the circle?
C. $(2, -7)$	c) What is the diameter of the circle?
9. Circle P is represented by this equation:	10. Circle O is represented by this equation:
$(x + 5)^2 + (y - 3)^2 = 40$	$(x - 2)^2 + (y + 3)^2 = 63$
What is the diameter of circle P2	Determine the center, radius and diameter
	Center Radius Diameter
A. 2√10	
B. 4√10	
C. 40 D. 80	
	(2, 3) (-2, 3) (2, -3) (-2, -3)
	31.5 6\sqrt{7} 126 3\sqrt{7}

Graph the Circle given the Equation-Day 6



Graph the Circle given the Equation-Day 6



#### **Coordinate Plane Circle Day 7**

Graph the following circles on the same coordinate plane, using graph paper and complete the table.

- 1. Circle C<sub>1</sub> has equation  $(x 3)^2 + (y 4)^2 = 25$ .
- 2. Circle  $C_2$  has center (0, 0) and radius 2.
- 3. Circle  $C_3$  has center (0, 0), and (-3, 4) is one point on the circle.
- 4. Circle  $C_4$  has center (-3, 0), and (-3, 2) is one point on the circle.
- 5. Circle  $C_5$  has center (3, 0) and is congruent to  $c_3$ .
- 6. (1, 0) and (-1, 0) are two points on a diameter of the circle C<sub>6</sub>.
- 7. Reflect circle  $C_6$  across the *x*-axis. The image is circle  $C_7$ .
- 8. Circle  $C_8$  has the following graph.



	(		A		В		4
		(					2
					C <sub>8</sub>		-1
-7 -	·6 -	-5 -	-4 -	-3 -	2 -	-1	0 1
							2

	center = ( <i>h, k</i> )	radius = <i>r</i>	List four points on the circle.	Equation of the Circle
C1				
C <sub>2</sub>				
C <sub>3</sub>				
<b>C</b> 4				
C <sub>5</sub>				
C <sub>6</sub>				
C <sub>7</sub>				
C <sub>8</sub>				

#### **Circles in the Coordinate Plane Day 7**

Graph the following equations. Then, answer the questions using the following vocabulary: center, diameter, radius, quadrant, *x*-axis, and *y*-axis.

1. Graph the equations  $x^2 + y^2 = 1$  and  $x^2 + y^2 = 4$  on the same graph. What is the difference between the two graphs? How does this relate to the difference between the two equations? Be specific.



2. Graph the equations  $x^2 + y^2 = 1$  and  $(x - 2)^2 + y^2 = 1$  on the same graph. What is the difference between the two graphs? How does this relate to the difference between the two equations? Be specific.



3. Graph the equations  $x^2 + y^2 = 1$  and  $x^2 + (y - 2)^2 = 1$  on the same graph. What is the difference between the two graphs? How does this relate to the difference between the two equations? Be specific.



4. Graph the equations  $x^2 + y^2 = 1$  and  $(x - 2)^2 + (y - 2)^2 = 1$  on the same graph. What is the difference between the two graphs? How does this relate to the difference between the two equations? Be specific.



### Day 8: Practice

1.	2.		
A circle has the equation $x^2 + y^2 = 16$ .	A circle has the equation		
What is the radius of the circle?	$(x + 5)^2 + (y - 2)^2 = 9$ . What is the		
<b>A.</b> 4	center of the circle?		
<b>B.</b> 16	<b>F.</b> (5, -2)		
<b>C.</b> 32	<b>G.</b> (-5, 2)		
<b>D.</b> 256	<b>H.</b> (2, -5)		
	I. (-2, 5)		
3.	4.		
A circle has the equation	What is the equation of a circle with		
$(x-3)^2 + (y+5)^2 = 36$ . Which of the following statements is NOT true?	center (2, 4) and radius 5?		
A The v seerdingte of the center is 2	<b>F.</b> $(x-2)^2 + (y-4)^2 = 5$		
A. The x-coordinate of the center is 5.	<b>G.</b> $(x + 2)^2 + (y + 4)^2 = 5$		
<b>B.</b> The y-coordinate of the center is 5.	<b>H.</b> $(x-2)^2 + (y-4)^2 = 25$		
C. The radius of the circle is 6.	1. $(x + 2)^2 + (y + 4)^2 = 25$		
<b>D.</b> The point (3, 1) lies on the circle.			
5.	6.		
. C is the center of the circle shown	C is the center of the circle shown		
below.	below.		
	(-2, -1) $(4, 7)$		
	What is the equation of circle $C$ ?		
	$A (x - 1)^{2} + (x - 3)^{2} = 100$		
	<b>B</b> $(x + 1)^2 + (y + 3)^2 = 100$		
	<b>C</b> $(x - 1)^2 + (y - 3)^2 = 25$		
What is the equation of circle C2	<b>D</b> $(x + 1)^2 + (y + 2)^2 = 25$		
<b>A</b> $(x - 2)^2 + (y + 1)^2 = 3$	<b>D.</b> $(x + 1) + (y + 3) - 25$		
<b>R</b> . $(x - 2)^2 + (y - 1)^2 = 3$			
(x + 2) + (y - 1) = 3			
$(y - 0)^{2} + (y + 1)^{2} - 0$			
<b>C.</b> $(x-2)^2 + (y+1)^2 = 9$			

#### **Day 8: Practice**

7. Which point lies on the circle whose equation is $(x - 3)^2 + (y + 3)^2 = 45$ ?	8. The center of a circle is at $(-5, 0)$ , and the diameter of the circle is 18. Which of the following is the equation of the	
F. (0, 3) G. (1, 3) H. (2, 3) I. (3, 3)	circle? <b>A.</b> $(x - 5)^2 + y^2 = 9$ <b>B.</b> $(x - 5)^2 + y^2 = 81$ <b>C.</b> $(x + 5)^2 + y^2 = 9$ <b>D.</b> $(x + 5)^2 + y^2 = 81$	
9. The center of a circle is at $(6, -7)$ and the diameter of the circle is 22. Which of the following is the equation of the circle? <b>F.</b> $(x - 6)^2 + (y + 7)^2 = 11$ <b>G.</b> $(x + 6)^2 + (y - 7)^2 = 11$ <b>H.</b> $(x + 6)^2 + (y - 7)^2 = 121$ <b>I.</b> $(x - 6)^2 + (y + 7)^2 = 121$	<b>10.</b> Which is the equation of a circle whose center is at the origin and that passes through the point (3, 5)? <b>F.</b> $(x - 3)^2 + (y - 5)^2 = 34$ <b>G.</b> $(x - 3)^2 + (y - 5)^2 = 64$ <b>H.</b> $x^2 + y^2 = 34$ <b>I.</b> $x^2 + y^2 = 64$	

#### 11.

Choose the expressions from the table below to correctly represent the equation of

the given circle:

A circle whose center is at (2, -5) and whose radius is 9

=

(x-2) <sup>2</sup>	(x+2) <sup>2</sup>	x <sup>2</sup>
(y-5) <sup>2</sup>	(y+5) <sup>2</sup>	y²
3	81	9

12. In the diagram,  $\overline{AB}$  is a diameter. Identify the center and the radius. Center: ( , ) Radius:



## **Day 9: Circles Practice**

<ul> <li>7.</li> <li>A circle with center (5, -3) has a radius of 4 units. Which point is on the circle?</li> <li>A (13, -3)</li> <li>B (9, 1)</li> <li>C (1, -7)</li> <li>D (5, 1)</li> </ul>	8. The endpoints of the diameter of a circle are (-3, 8) and (-5, 4). What is an equation of the circle? A $(x + 4)^2 + (y - 6)^2 = 20$ B $(x - 4)^2 + (y + 6)^2 = 25$ C $(x + 4)^2 + (y - 6)^2 = 100$ D $(x + 4)^2 + (y - 6)^2 = 5$
9. Circle A has equation $(x - 5)^2 + (y + 1)^2 = 16$ . What is the center and radius of the circle?	10. Identify the center, radius and diameter of a circle with the equation $(x - 1)^2 + (y + 4)^2 = 81$
11. Given point on a circle at (1, -7) and a center at (-6, -4), write the equation of the circle.	12. Circle O is defined by the equation $x^2 + (y-2)^2 = 25$ Plot the center of circle O and one point with integral coordinates that lies on the circle.
13.         Give the equation of the circle $(x + 5)^2 + (y - 1)^2 = 16$ , which correctly         gives the center and radius of the circle?         A. $(5, -1); r = 4$ C. $(5, -1); r = 8$ B. $(-5, 1); r = 4$ D. $(-5, 1); r = 8$	14. A circle with a center at (2, -3) passes through the point (-1, -8). Write the equation of the circle. A. $(x - 2)^2 + (y + 3)^2 = 34$ B. $(x + 2)^2 + (y - 3)^2 = 34$ C. $(x - 2)^2 + (y + 3)^2 = 17$ D. $(x + 2)^2 + (y - 3)^2 = 17$

Day 10

On your graph paper, you must create a picture using circles. You must use at least 4 circles in your picture. You must also provide the equations of each circle, the center and the radius.



Journal/Writing Prompt: Explain how you would find the equation of a circle whose graph is given.